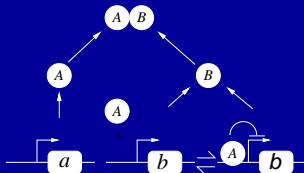


# Structure des petits réseaux génétiques et évolution *in silico*

Paul François (thèse) Hervé Rouault (thèse)

Laboratoire de Physique Statistique, CNRS & ENS, Paris .

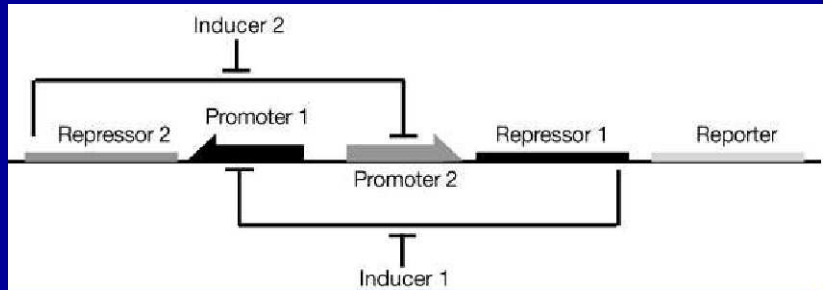


## Genetic networks.

- Dynamics in a cell: bistability, oscillations (circadian , ...)
- Spatial patterns (C. elegans, somites,...)
- Coordinated evolution of several genes/proteins.
- Design of synthetic modules.

# A synthetic genetic switch

Two genes  $a$  and  $b$  that inhibit each other. Two stable steady states :  $[A]$  high with  $[B]$  low, and  $[B]$  high with  $[A]$  low.

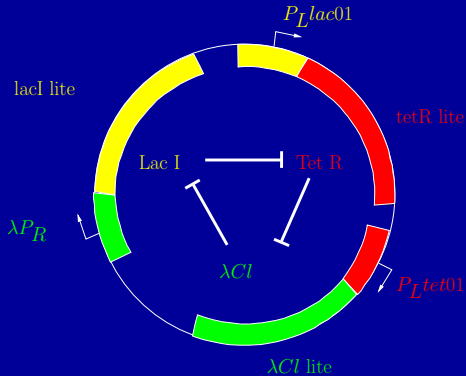


Switching can be induced by an IPTG or a temperature pulse.

Gardner et al, *Nature* 403:339-342 (2000)

Bistability requires dimerizations (or other interactions).

# A synthetic genetic ring oscillator

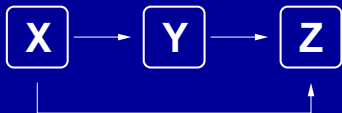


The oscillation is based on three genes that repress each other in a circle (“rock-scissor-paper”).

M. Elowitz and S. Leibler, *Nature* 403:335-338 (2000)

- ▶ What are the designs that achieve a given function?
- ▶ Can one sample them and add desired constraints (robustness,...) ?
- ▶ Easyness of creation, evolvability,...?
- ▶ Blueprints of useful networks.

## An overrepresented motif in transcriptional networks



The “feedforward loop” is overrepresented in the transcriptional networks of *E. Coli* and *S. Cerevisiae* (Milo et al., *Science* 298: 824-827(2002)).

Function: a persistence detector?

## Proposal : design by selection *in silico*.

The inverse of the statistical approach: from the desired task to the network.



To design modules performing given tasks (e.g. switches and oscillators), without imposing *a priori* any structure to the network, one evolves a collection of virtual “cells”.

P. François and V. Hakim, *PNAS*, **101** 580-585 (2004).

One computer 'cell' consists in





One computer 'cell' consists in

- a collection of genes 
- and associated proteins 

First implementation: transcription and translation condensed in one single step.

mRNA are included in the present version.

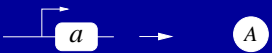
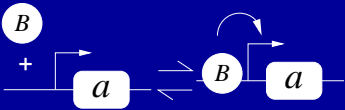
One computer 'cell' consists in

- a collection of genes 
- and associated proteins 

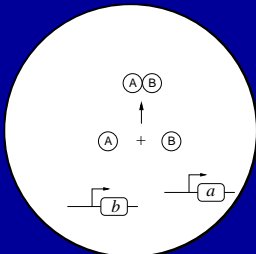
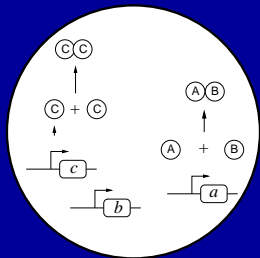
First implementation: transcription and translation condensed in one single step.

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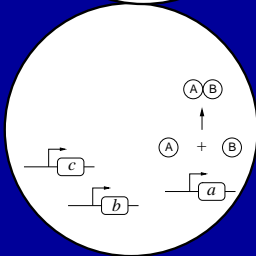
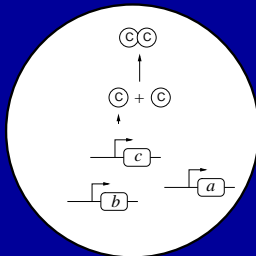
- transcriptional regulations 
- **post-transcriptional** regulations. 

Representation	Corresponding equations
	$\frac{d}{dt}[A] = \tau_A[a] - \delta_A[A]$
	$\begin{aligned} \frac{d}{dt}[a] &= \theta[a : B] - \gamma[a][B] \\ \frac{d}{dt}[a : B] &= \gamma[a][B] - \theta[a : B] \\ \frac{d}{dt}[A] &= \tau_A[a] + \tau'_A[a : B] \end{aligned}$

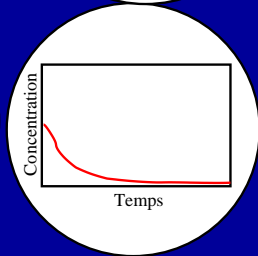
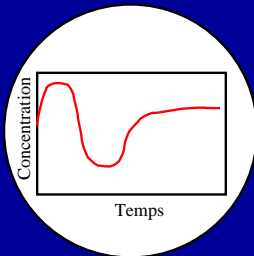
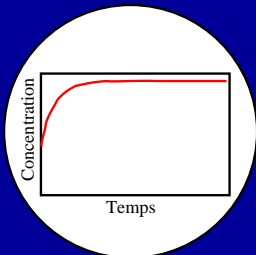
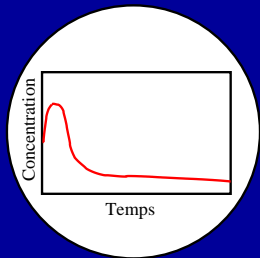
# The evolution *in silico*.



Cells

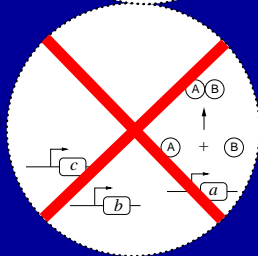
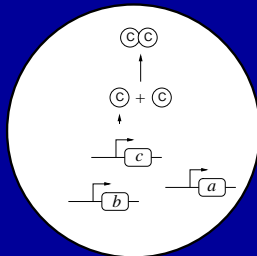
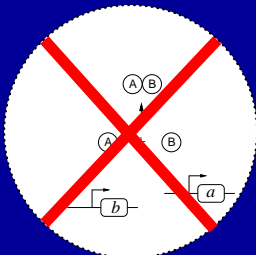
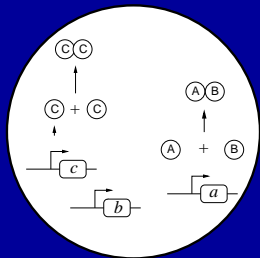


# The evolution *in silico*.



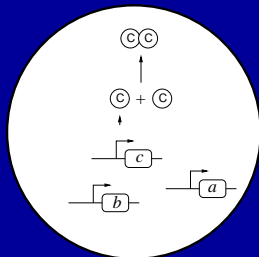
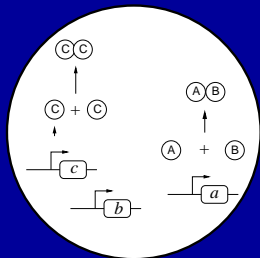
Integration of ODEs

# The evolution *in silico*.



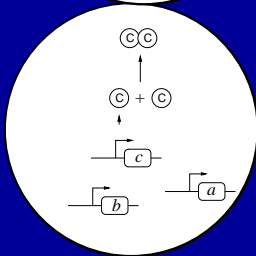
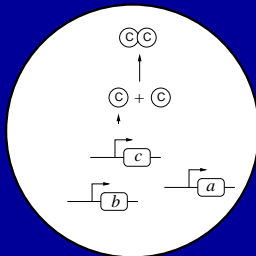
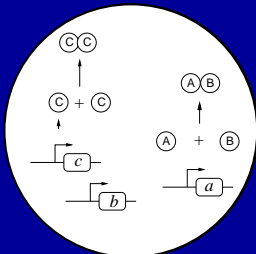
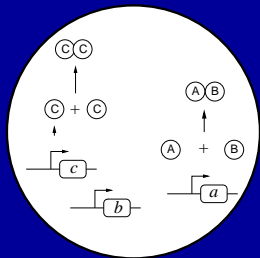
Selection

# The evolution *in silico*.



Elimination

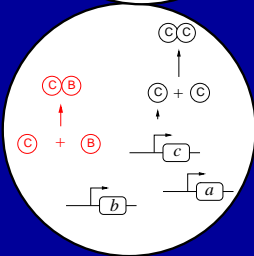
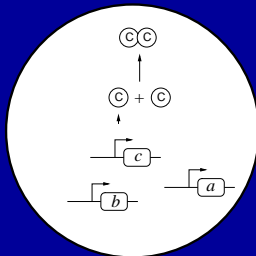
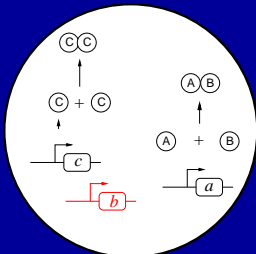
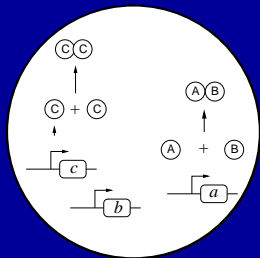
# The evolution *in silico*.



Duplication



# The evolution *in silico*.



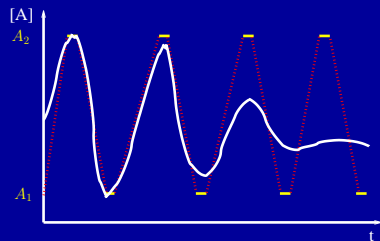
Mutations

## Possible mutations

- ▶ The modification of a kinetic constant in an existing reaction
- ▶ or the addition of
- ▶ A new transcriptional regulation
- ▶ A new post-transcriptional regulation
- ▶ A new gene

**The process is iterated over several generations.**

## Fitness function for oscillators



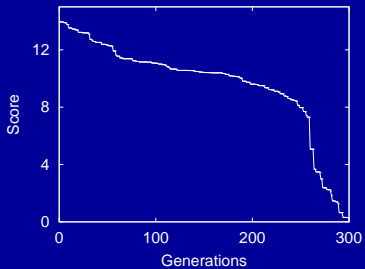
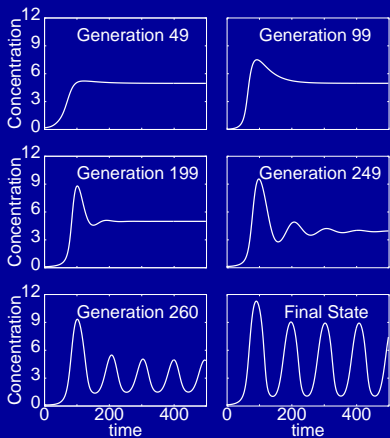
Two concentrations are fixed  $A_1$  and  $A_2$ .

ODEs are integrated

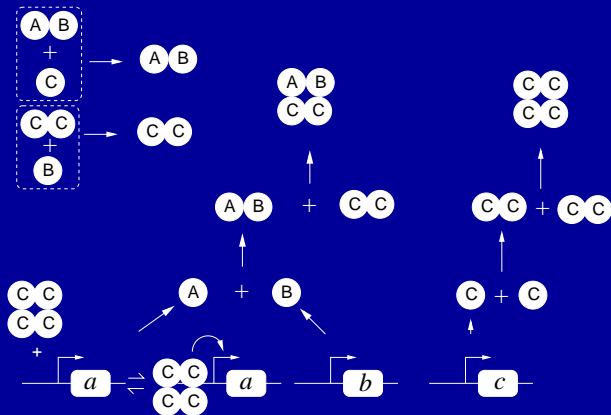
For  $t = T/2, 3T/2, 5T/2 \dots$  fitness is given by the integral  $(A - A_1)^2$ .

For  $t = T, 2T, 3T \dots$  fitness is given by the integral  $(A - A_2)^2$ .

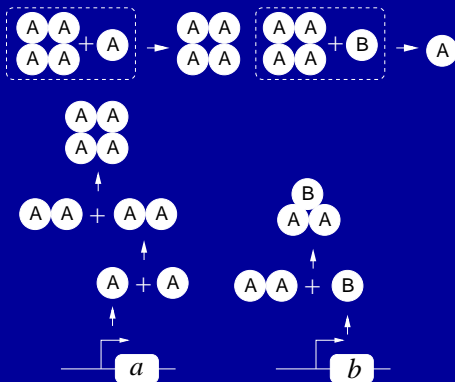
# Fitness evolution



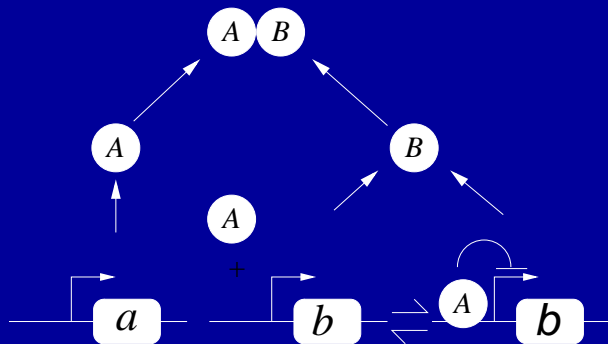
# The oscillating network



# A purely biochemical oscillator

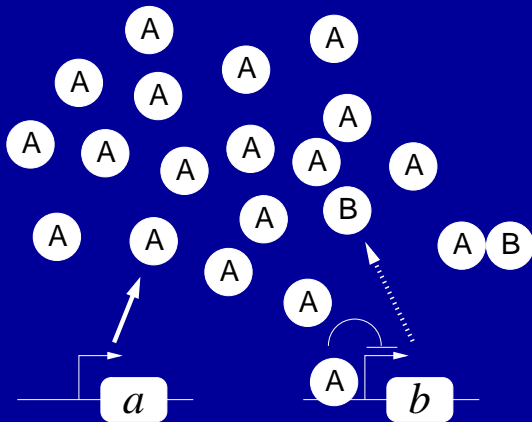


## A created bistable switch



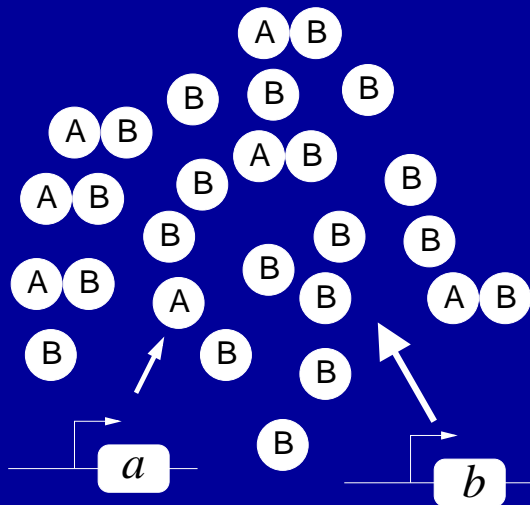
Very different from two genes with reciprocal inhibition

## A created bistable switch



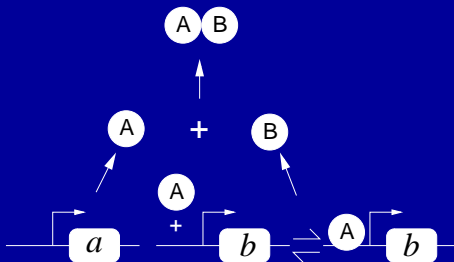


## A created bistable switch



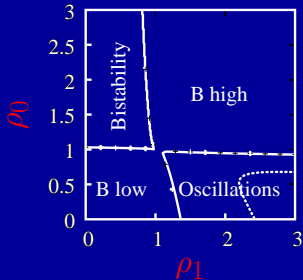
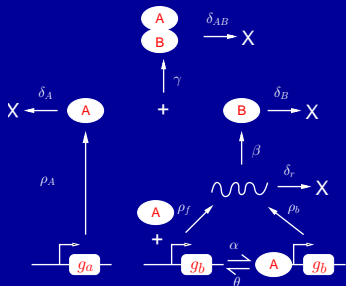
## A core genetic circuit: the Mixed Feedback Loop

**A loop** combining transcriptional and post-transcriptional interaction (i.e. protein-protein interaction) is **at the core** of several of these networks.



This **Mixed Feedback Loop** has now been found to be **over-represented** in *S. Cerevisiae* and *E. Coli* (Yeager-Lotem et al, PNAS 2004).

# Mathematical analysis of the MFL



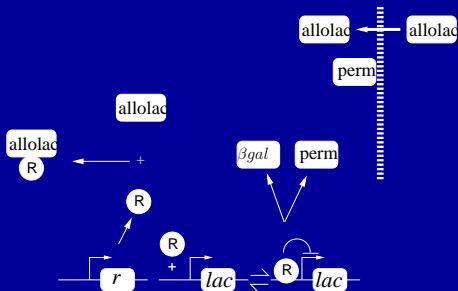
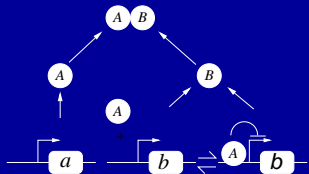
Reduced parameters:  $\rho_0 = \beta \rho_f / (\rho_A \delta_r)$ ,  $\rho_1 = \beta \rho_b / (\rho_A \delta_r)$

A small parameter:  $\delta_r / \sqrt{\rho_A \gamma}$

( P. François and V. Hakim, PRE (2005)

# Comparison with real networks

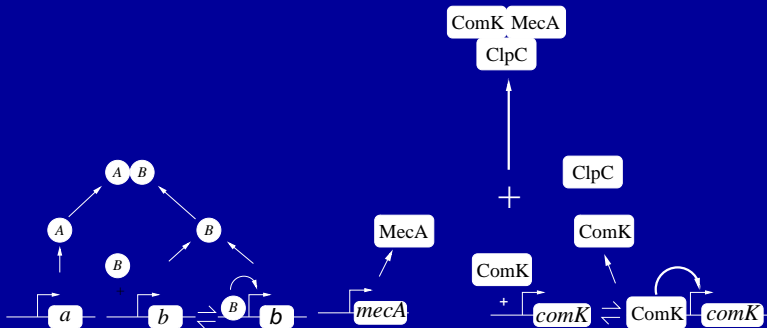
First switch: lactose operon, with allolactose binding to lac repressor.



Proposed in 1961 by Monod and Jacob (based on Lac operon) as an alternative to reciprocal inhibition (Delbrück, 1949) !

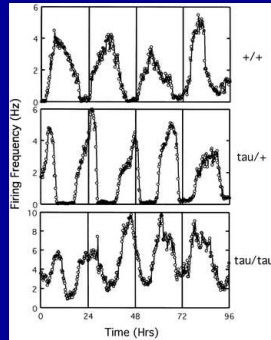
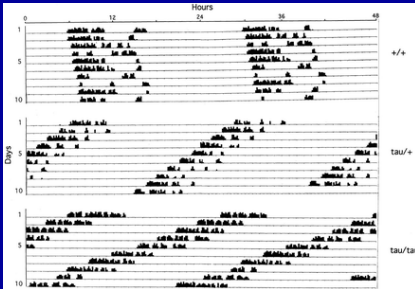
## Comparison with real networks

Second switch: developpement of competence in *B.subtilis* ,  
Comk activates itself and is repressed by MecA.

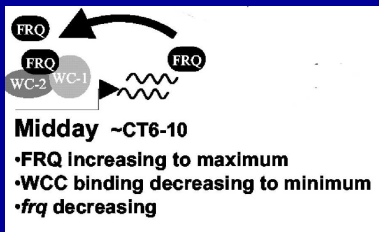


# Endogenous oscillator : the circadian clock

Circadian activities of whole animals and single cells  
Liu et al, Cell (1997)



# The core structure of circadian clocks



Froehlich et al, PNAS (2003)

Organism	Activators A	Repressors B
Neurospora Crassa	WC-1, WC-2	FRQ
Drosophila	dCLK	PER, TIM
Mammals	CLOCK, BMAL	PER, CRY

The created networks are working examples without delays or high Hill coefficients  $\Rightarrow$  motivation for **new models** of the circadian rhythms [for *Neurospora*, P. François Biophys. J. **88**, 2369 (2005)].

The algorithm finds known (with complete description) and original designs.

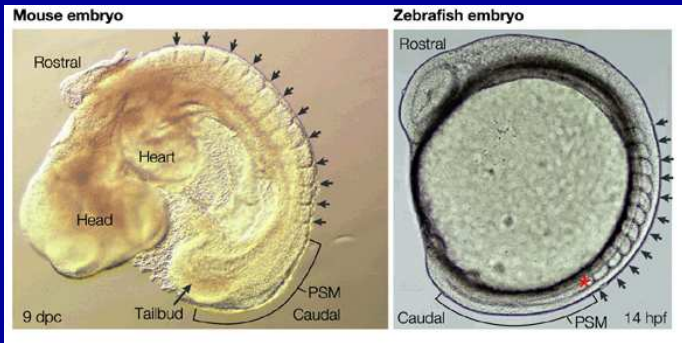
**An important lesson:** The post-transcriptional interactions play a crucial role: the function of the networks cannot be understood at all by focusing only on the transcriptional regulations (**protein sequestration** in a complex appears to be a particularly important mechanism).

## Work in progress/Perspectives

- Analysis of specific features of some genetic networks (e.g. temperature compensation).
- Blueprint for new synthetic networks.
- Evolution of real genetic networks.
- Spatial patterns, morphogenesis.



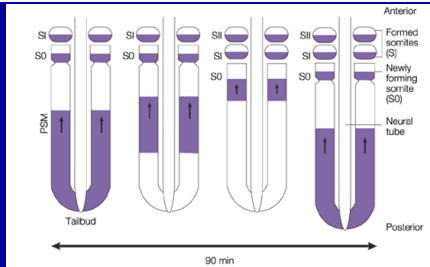
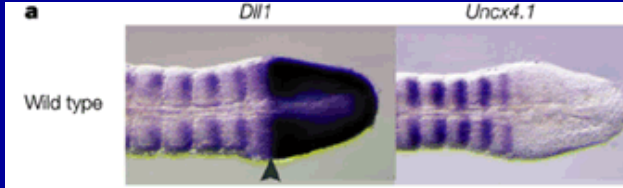
# Somites



Y. Saga, Nat. Rev. Gen. (2001)

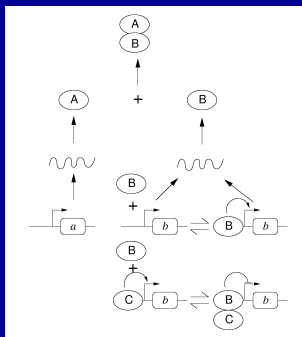
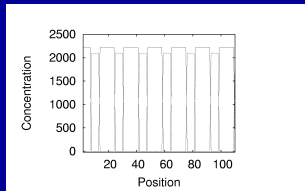
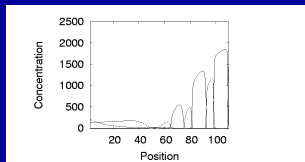
# Somitogénèse et oscillations

(Cooke & Zeeman (1976) → Palmeirim et al (1997))



Y. Saga, Nat. Rev. Gen. (2001)

# Segmentation as an oscillating/bistable transition?



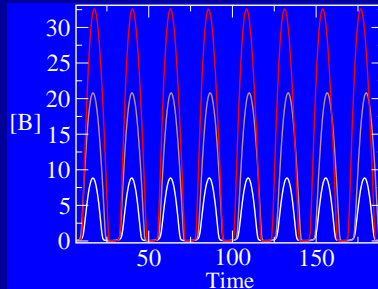
The End (for today).

Thank you!

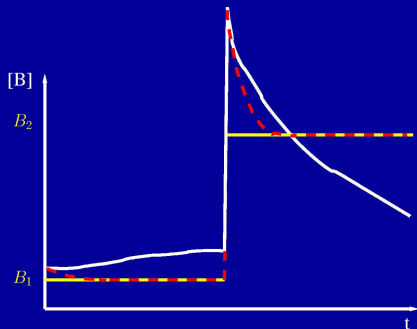
# Temperature compensation

Selection of activation energies for temperature compensation:

- a  $10^\circ K$  increase :  $T : 300^\circ K \rightarrow 310^\circ K$
- the kinetic constants increase  $> 30\%$ ,
- period change  $< 3\%$ .

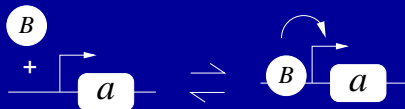


# Fitness function for the switches

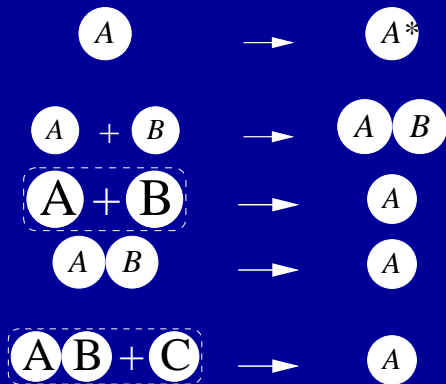


The desired two stable states are chosen  $(A_1, B_1)$  and  $(A_2, B_2)$ . ODEs are integrated, the “fitness” is given by the integral  $(A - A_1)^2 + (B - B_1)^2$ . Pulse of B protein ODEs are integrated, the fitness is given by the integral  $(A - A_2)^2 + (B - B_2)^2$ .

# Transcriptional regulations

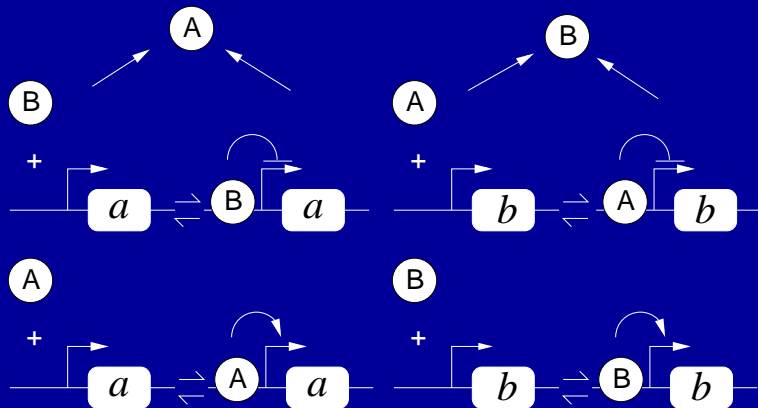


# Post-transcriptional regulations

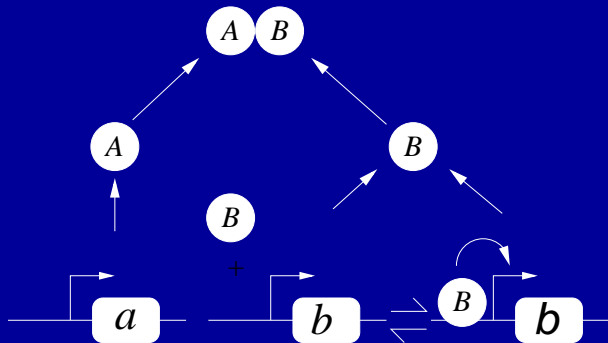




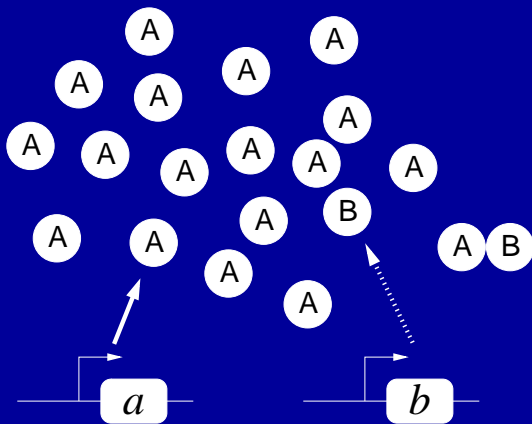
# Transcriptional switches



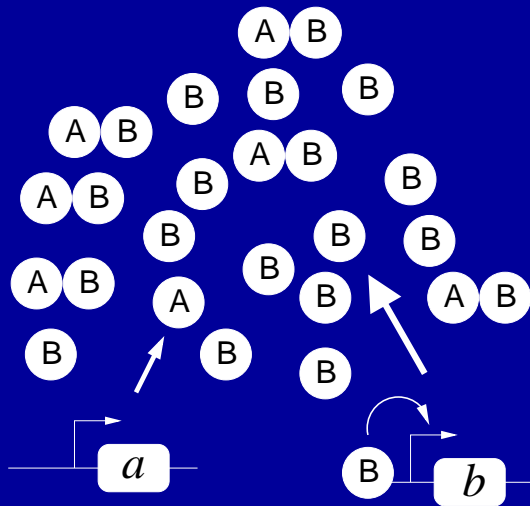
## A second type of switch



## A second type of switch



## A second type of switch



# 'Toggle' switch : mathematical analysis

$$\frac{dA}{dt} = \frac{\alpha}{B_0 + B^\nu} - \delta_A A$$

$$\frac{dB}{dt} = \frac{\beta}{A_0 + A^\mu} - \delta_B B$$

$\nu$   $\mu$  must be strictly higher than 1 to have bistability, which requires at least *four* (and not two) elementary reactions.

[Cherry and Adler, J. Theor. Biol. (2000)]

